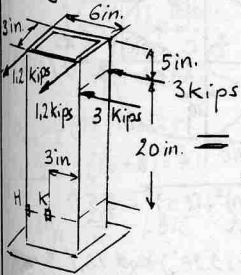


6.26 Equivalent Force-couple system in section

through H and K:

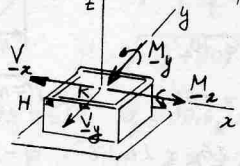


$$V_x = 2(3 \text{ kips}) = 6 \text{ kips}$$

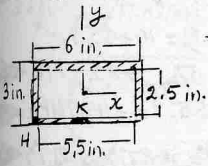
$$V_y = 2(1.2 \text{ kips}) = 2.4 \text{ kips}$$

$$M_y = (6 \text{ kips})(20 \text{ in.}) = 120 \text{ kip}\cdot\text{in.}$$

$$M_x = (2.4)(25) = 60 \text{ kip}\cdot\text{in.}$$



Properties of section



$$A = 6 \times 3 - 5.5 \times 2.5 = 4.25 \text{ in}^2$$

$$I_x = \frac{1}{12} (6 \times 3^3 - 5.5 \times 2.5^3) = 6.3385 \text{ in}^4$$

$$I_y = \frac{1}{12} (6^3 \times 3 - 5.5^3 \times 2.5) = 19.3385 \text{ in}^4$$

(a) Stresses at H:

$$\sigma_x = 0, \sigma_z = -\frac{M_x(1.5 \text{ in.})}{I_x} - \frac{M_y(3 \text{ in.})}{I_y} = -\frac{60 \times 1.5}{6.3385} - \frac{120 \times 3}{19.3385}$$

$$\sigma_z = -14,199 - 18,616 = -32,815 \text{ ksi}$$

Since H is at corner:  $\tau_{xz} = 0$

Maximum shearing stress:

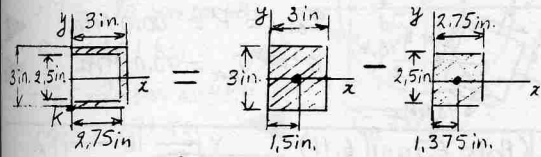
$$\text{Eq. (6.16): } \tau_{\max} = \sqrt{\left(\frac{\sigma_x - \sigma_z}{2}\right)^2 + \tau_{xz}^2} = \frac{32,815}{2}$$

$$\tau_{\max} = 16,41 \text{ ksi}$$

Planes of max. shearing stress:

Since  $\tau_{xz} = 0$ , the principal axes are the x and z axes. The planes of max. shearing stress are at  $45^\circ$  to the principal axes:  $45,0^\circ$  and  $45,0^\circ$

(b) Stresses at K: For computation of  $\tau_{xz}$ :



$$Q_y = \Sigma A \bar{x} = (3 \text{ in.})(1.5 \text{ in.}) - (2.75 \text{ in.} \times 2.5 \text{ in.})(1.375 \text{ in.})$$

$$Q_y = 4.0469 \text{ in}^3$$

$$t = 3 \text{ in.} - 2.5 \text{ in.} = 0.5 \text{ in.}$$

$$\sigma_z = -\frac{M_x(1.5 \text{ in.})}{I_x} = -\frac{60 \times 1.5}{6.3385} = -14,199 \text{ ksi}$$

$$\tau_{xz} = -\frac{V_x Q_y}{I_y t} = -\frac{6 \times 4.0469}{19.3385 \times 0.5} = -2,5112 \text{ ksi}$$

Maximum shearing stress:

$$\text{Eq. (6.16): } \tau_{\max} = \sqrt{\left(\frac{14,199}{2}\right)^2 + (2,5112)^2} = 7,53 \text{ ksi}$$

Planes of max. shearing stress:

$$\text{Eq. (6.15): } \tan 2\theta_s = -\frac{\sigma_x - \sigma_z}{2\tau_{xz}} = -\frac{0 - (-14,199)}{2(-2,5112)}$$

$$= +2,82713$$

$$2\theta_s = 70,52^\circ \text{ and } -109,48^\circ \quad \theta_s = 35,3^\circ \text{ and } 54,7^\circ$$