

6-27 For the loading scheme shown in Figure (c),

$$M_{\max} = \frac{F}{2} \left(\frac{a}{2} + \frac{b}{4} \right) = \frac{4.4}{2}(6 + 4.5) \\ = 23.1 \text{ N} \cdot \text{m}$$

For a stress element at A:

$$\sigma_x = \frac{32M}{\pi d^3} = \frac{32(23.1)(10^3)}{\pi(12)^3} = 136.2 \text{ MPa}$$

The shear at C is

$$\tau_{xy} = \frac{4(F/2)}{3\pi d^2/4} = \frac{4(4.4/2)(10^3)}{3\pi(12)^2/4} = 25.94 \text{ MPa}$$

$$\tau_{\max} = \left[\left(\frac{136.2}{2} \right)^2 \right]^{1/2} = 68.1 \text{ MPa}$$

Since $S_y = 220 \text{ MPa}$, $S_{s_y} = 220/2 = 110 \text{ MPa}$, and

$$n = \frac{S_{s_y}}{\tau_{\max}} = \frac{110}{68.1} = 1.62 \quad \text{Ans.}$$

For the loading scheme depicted in Figure (d)

$$M_{\max} = \frac{F}{2} \left(\frac{a+b}{2} \right) - \frac{F}{2} \left(\frac{1}{2} \right) \left(\frac{b}{2} \right)^2 = \frac{F}{2} \left(\frac{a}{2} + \frac{b}{4} \right)$$

This result is the same as that obtained for Figure (c). At point B, we also have a surface compression of

$$\sigma_y = \frac{-F}{A} = \frac{-F}{bd} = \frac{-4.4(10^3)}{18(12)} = -20.4 \text{ MPa}$$

With $\sigma_x = -136.2 \text{ MPa}$. From a Mohr's circle diagram, $\tau_{\max} = 136.2/2 = 68.1 \text{ MPa}$.

$$n = \frac{110}{68.1} = 1.62 \text{ MPa} \quad \text{Ans.}$$

